

Using Directed Acyclic Graphs (DAGs) to Advance Causal Inference with Observational Data

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Before we start...

I would like to know a bit about your background and knowledge:

- Master's / PhD student / Researcher ?
- Geography / Communication / Politics / Psychology / Social Policy / Sociology
- Regression / confounding / fundamental problem of causality / colliders

Outline

A) Counterfactuals, causal inference and observational data

- The counterfactual model of causality
- The fundamental problem of causal inference
- Assignment and the conditional independence assumption
- B) Basics of directed acyclic graphs
 - Terminology and core concepts
 - Fundamentals of analyzing causal graphs
 - Identification strategies

C) DAGs in action

- Exemplary application: weight and wages
- Analyzing causal graphs with the software DAGitty
- Short exercise

Part A Counterfactuals, Causal Inference and Observational Data

Counterfactual causality

The basic idea can be already found in work by John Stuart Mill (1806-1873)

"Thus, if a person eats of a particular dish, and dies in consequence, that is, would not have died if he had not eaten of it, people would be apt to say that eating of that dish was the cause of his death."

Source: John Stuart Mill (2002). A System of Logic. Reprinted from the 1981 edition (first published 1843). Honolulu: UP of the Pacific. S. 214.



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The counterfactual model

Building on early work by John Stuart Mill, Jerzy Neyman and others, Donald Rubin (1974, 1977, 1978) formalized these ideas

Starting point:

- Binary treatment
 - D = 1 treatment (treatment group)
 - D = 0 no treatment (control group)
- "Outcome" variable Y: continuous

At least theoretically, each unit could be observed in two states: \rightarrow Potential outcomes $\left(Y_i^0, Y_i^1\right)$

Journal of Educational Psychology 1974, Vol. 66, No. 5, 688-701

ESTIMATING CAUSAL EFFECTS OF TREATMENTS IN RANDOMIZED AND NONRANDOMIZED STUDIES¹

DONALD B. RUBIN² Educational Testing Service, Princeton, New Jersey



Counterfactual model: individual treatment effect

Defining causal effects I: Individual treatment effect (ITE)

$$ITE = \delta_i = Y_i^1 - Y_i^0$$

 \rightarrow the causal effect of treatment D on outcome Y for study unit i is defined as the difference between the two potential outcomes in the experimental and control condition

Counterfactual model: average treatment effect

Defining causal effects II: Average treatment effect (ATE)

$$ATE = \frac{\sum \delta_i}{n} = \frac{\sum_{i=1}^n Y_i^1 - Y_i^0}{n}$$
$$= E(Y_i^1 - Y_i^0)$$
$$= E[Y_i^1] - E[Y_i^0]$$

→ the average treatment effect (ATE) at group level is thus the mean of the individual treatment effects

- Experimental group (D = 1): Individuals in the experimental condition committed to severely reducing their social media use for one month.
- Control group (D = 0): individuals in the control condition can use social media without restrictions.
- The ability to concentrate is measured by means of a validated test after one month and can have values from 0 (very poor) to 100 (very good).

 \rightarrow There are thus two potential outcomes for each participant:

- the ability to concentrate after a one-month break Y^1
- the ability to concentrate without this intervention Y^0

In reality, we would measure "ability to concentrate" from 0 (very poor) to 100 (very good) with the following observed outcomes (denoted by lower y)

		y^1	<i>y</i> ⁰	δ_i
<i>D</i> = 1	<i>i</i> = 1	90	missing	
	<i>i</i> = 2	60	missing	
	Ø (<i>D</i> = 1)	75	60	
D = 0	<i>i</i> = 3	Missing	80	
	<i>i</i> = 4	Missing	60	
	<i>i</i> = 5	Missing	60	
	\emptyset ($D = 0$)	75	66,7	

 \rightarrow let's assume we are in a hypothetical world, in which we can observe all the potential outcomes (denoted by capital Y)

The following table contains potential outcomes

		Y ¹	<i>Y</i> ⁰	δ_i
<i>D</i> = 1	<i>i</i> = 1	90	80	
	<i>i</i> = 2	60	40	
	Ø ($D = 1$)	75	60	
D = 0	<i>i</i> = 3	80	80	
	<i>i</i> = 4	75	60	
	<i>i</i> = 5	70	60	
	\emptyset ($D = 0$)	75	66,7	

Y^1 Y^0 δ_i individual treatment effects (ITE) $D=1$ $i=1$ 908010 $i=2$ 604020 \emptyset ($D=1$)756015 $D=0$ $i=3$ 80800 $i=4$ 756015 $i=5$ 706010 \emptyset ($D=0$)7566,78,3							
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$			Y^1	<i>Y</i> ⁰	δ_i		individual treatment effects (ITE)
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	<i>D</i> = 1	i = 1	90	80	10] .	
\emptyset (D = 1)756015i = 1:90 - 80 = 10D = 0i = 380800i = 4756015i = 5706010 \emptyset (D = 0)7566,78,3		<i>i</i> = 2	60	40	20		$ITE = \delta_i = Y_i^1 - Y_i^0$
$D = 0 i = 3 \qquad 80 \qquad 80 \qquad 0 \qquad \cdots$ $i = 4 \qquad 75 \qquad 60 \qquad 15 \qquad \cdots$ $i = 5 \qquad 70 \qquad 60 \qquad 10 \qquad \text{average treatment effect (ATE)}$		\emptyset ($D = 1$)	75	60	15		i = 1: 90 - 80 = 10
$i = 4$ 75 60 15 $i = 5$ 70 60 10 $\emptyset (D = 0)$ 75 66,7 8,3 average treatment effect (ATE)	D = 0	<i>i</i> = 3	80	80	0		
$i = 5$ 706010 $\emptyset (D = 0)$ 7566,78,3average treatment effect (ATE)		<i>i</i> = 4	75	60	15		
O(D=0) 75 66,7 8,3 average treatment effect (ATE)		<i>i</i> = 5	70	60	10		
		$\emptyset (D=0)$	75	66,7	8,3		average treatment effect (ATE)

$$ATE = \frac{\sum \delta_i}{n} = (10 + 20 + 0 + 15 + 10) / 5 = 11$$

- The individual causal effect is theoretically clearly defined, but we cannot observe the same unit of study in two different states at one point in time
- observed outcome (as opposed to potential outcome): only one potential outcome can be observed at a time (= factual state).
- the assignment mechanism D determines which one is observed

$$Y_i = D_i Y_i^1 + (1 - D_i) Y_i^0$$

$$\Rightarrow Y_i = Y^1 \qquad \text{für D=1}$$

$$\rightarrow$$
Y_i = Y⁰ für D=0

To distinguish between potential and observed outcomes, observed outcomes are sometimes written as lower y (as compared to the potential outcome as capital Y)

• Paul Holland (1986) called this the fundamental problem of causal inference

	Υ ¹	Υ ⁰
D=1	factual (observed)	counterfactual (unobserved)
D=0	counterfactual (unobserved)	factual (observed)

• We can re-write this as conditional expected values

	Y ¹	Yo
D=1	E[Y ¹ D=1]	E[Y ⁰ D=1]
D=0	E[Y ¹ D=0]	E[Y ⁰ D=0]

As explained, one would calculate the average treatment effect (ATE) as follows:

$$ATE = \frac{\sum \delta_i}{n} = E(Y_i^{1} - Y_i^{0}) = E[Y_i^{1}] - E[Y_i^{0}]$$

This can be re-written as:

$$ATE = \{\pi E[Y^{1}|D = 1] + (1 - \pi)E[Y^{1}|D = 0]\} \\ -\{\pi E[Y^{0}|D = 1] + (1 - \pi)E[Y^{0}|D = 0]\}$$

with $\pi = E(D)$ as the relative size of the treatment group as compared to the overall sample size

- \rightarrow if treatment and control group have equal size π =0.5
- \rightarrow In our social media example, treatment group is π = 2/5 =0.4

$$ATE = \{\pi E[Y^{1}|D = 1] + (1 - \pi)E[Y^{1}|D = 0]\} \\ -\{\pi E[Y^{0}|D = 1] + (1 - \pi)E[Y^{0}|D = 0]\}$$

- \rightarrow Essential information is missing for calculating the ATE.
- → Causal inference as a missing data problem!
- \rightarrow The same holds for the ITE.
- → As a consequence, one <u>always</u> has to make <u>assumptions</u> for identification. This illustrates the central role of assumptions and uncertainty in causal inference.

Observational, not experimental data

Very often we do not have experimental data.

For example, we might want to analyze data for

- Individuals i who use social media heavily $(d_i=1)$
- Individuals j who use social media less often (d_i=0)

Suppose we

- have a measure Y about their ability to concentrate (from a survey or test)
- decide to compare average Y for the two groups

Estimator: naïve average treatment effect (NATE)

With groups of treated and controls, one might try to estimate the ATE as follows:

 $\widehat{ATE} = E[y_i | d_i = 1] - E[y_j | d_j = 0]$

- → This simple comparison of treated and controls rarely leads to the correct estimate (exception experiment). Some call it the **naïve average treatment effect (NATE)**
- → If we compare this with the correct equation, a core assumption becomes clear, namely that treatment and control group are comparable.



We use one group to approximate the counterfactual value for the other group.

Estimator: naïve average treatment effect (NATE)

The NATE will provide bias in case of selection

 $NATE = E[Y^{1}|D = 1] - E[Y^{0}|D = 0]$ = $ATE + \underbrace{E[Y^{0}|D = 1] - E[Y^{0}|D = 0]}_{\text{baseline bias}} + (1 - \pi) \underbrace{(ATT - ATC)}_{\text{treatm. effect bias}}$ selection bias

selection bias = baseline bias + $(1 - \pi)^*$ treatment effect bias

In our example of social media use:

- Baseline bias: before the treatment both groups might differ in Y
- Treatment effect bias: social media use might affect Y differently for both groups

The conditional independence assumption

• The key requirement for unbiasedness is the **conditional independence assumption (CIA)**

$$\left(Y^0,Y^1\right)\perp D\Big|X$$

- If the CIA holds, the conditional NATE (that is the NATE after conditioning for all relevant Xs) provides an unbiased estimate of the ATE
- But there is no proof that the CIA actually holds

The assignment mechanism

• Since selection leads to biases, estimation of causal effects of a treatment (usually) starts with studying the selection process, also known as **assignment mechanism**

$$Y_{i} = D_{i}Y_{i}^{1} + (1 - D_{i})Y_{i}^{0}$$

- In our example:
 - Which type of individuals use social media how?
 - Which factors explain variation in social media use?
 - Age?
 - Education?
 - ...

The conditional independence assumption

What does the CIA imply for working with observational data?

 $(Y^0, Y^1) \perp D | X$

 \rightarrow Guided by intuition, theory, and previous reserach identify all Xs that are relevant

- \rightarrow But: not just include every X that comes to your mind, but draw a DAG!
- ightarrow ex post adjustment for these X variables
 - Stratification (e.g., subgroup analyses, crosstables etc.)
 - Regression (condition on X),
 - Matching (Compare individuals with same/similar X values),
 - Weighting (Weigh T and C in a way that X values are balanced)

 \rightarrow conditional NATE

Part B Basics of Directed Acyclic Graphs

Directed acyclic graphs (DAGs)

- Popular framework in machine learning, statistics, ulletand increasingly the social and behavioral sciences
- Graphical representation of causal relationships ٠ \rightarrow visualizes your causal assumptions
- Proposed and advanced by Pearl (2000, 2009, 2019)
- At first glance similar to classical structural equation ulletmodels, but in contrast to SEMs, no assumptions about functional form of relationships \rightarrow nonparametric structural equation model (e.g. Y = f(Z))
- Focus on identification of causal effects treating ۲ estimation as a distinct step



WILEY



Lundberg et al. 2021, p. 534

Concepts/terminology

- Nods depict random variables.
- Variables can be observed or unobserved o
- <u>Directed</u> edges (arrows) connect nods
- Bidirectional edges are a shorthand for mapping a common influence
- Graphs need to be <u>acylic</u>
- \rightarrow No cycles
- ightarrow No mutual causality at T



→ Drawing a DAG is equivalent to specifying a joint probability distribution of the variables involved in the system (Bayesian network/Hidden Markov Model)

Open paths as a source of bias

A **path** is any connection between two nods via edges irrespective of their direction.

Paths can be:

- direct $(X \rightarrow Y)$ or indirect $(X \rightarrow M \rightarrow Y)$.
- causal (X \rightarrow M \rightarrow Y) or non-causal (X \leftarrow Z \rightarrow Y or X \rightarrow Z \leftarrow Y). [non-causal if at least one arrow points toward T]
- front door path (X → M → Y; note: all arrows run towards Y) and back door path (D←Z→Y, D←Z→V←Y, note: at least one arrow does not run towards Y)

Front door paths and – open or closed – back door paths

Causality flows through **front door** paths:

 $X \rightarrow Y$

 $X \rightarrow M \rightarrow Y$

Biases <u>potentially</u> flow through **back door** paths:

 \rightarrow A back door path is a source of bias if it is **open**.

 $D \leftarrow Z \rightarrow Y$ or $D \leftarrow Z1 \rightarrow Z2 \rightarrow Y$

 \rightarrow To eliminate bias, you should **close** open paths.

 $D \leftarrow Z \rightarrow Y \rightarrow D \leftarrow Z \rightarrow Y$

 \rightarrow Beware: some back door paths are already closed, but you might open them

 $D \rightarrow C \leftarrow Y \rightarrow D \rightarrow C \leftarrow Y$

Reading Assumptions in a DAG



What are the assumptions in this DAG?

- No edge from U to D
- No edge from Y to U, D to X, D to U ... (cycles)

Indeed, all variables except for D and U are already directly connected

Correlation and causality

- Starting point: a correlation between two variables implies that some causal process is going on
- ... but not necessarily that one of the two variables causally affects the other
- In a DAG, a correlation implies that there is at least one **open path** between these two variables
- If there is no correlation, then there is either no path or all paths are **blocked**, this is called **d-separated**
 - \rightarrow testable implication of a DAG: zero correlation

Open and blocked paths

Obviously, a direct effect from A to B (A \rightarrow B) causes an open path. However, a path between A and B can also exist due to third variables

Structural positions of covariates

- Confounder
- Collider
- Mediator/intervening variable
- \rightarrow Position affects whether a path is open / closed and hence how to deal with this X
- → Unfortunately, in more complex graphs a variable can have different structural positions at the same time (which can complicate things quite a bit....)

Confounder: A well-known problem

- Common understanding: covariate is associated with treatment and outcome.
- Including this covariate in the model changes the causal effect of interest.
- \rightarrow Definition too broad: Also includes covariates whose control leads to bias!

Pearl's concept of the back door path



] : means that you adjust/control/condition for the variable

Collider: over-control, missing data and selection effects.

• Reverse scenario to the confounder



- well-intended covariate adjustment
 - \rightarrow leads to biased estimates
 - → obviously, we need to move away from a "control everything that could potentially be relevant in some way" strategy

Closing open backdoor paths

When should I control for a variable on the path from X to Y?

 \rightarrow Backdoor criterion: We need to block all open non-causal paths from treatment to outcome



Which ones are open? Which are already closed?

- \rightarrow Confounder leads to open backdoor path \rightarrow control for it
- ightarrow Collider leads to closed backdoor path ightarrow don't control for it

Collider

- many distortions that have been treated rather disparately so far are special collider problems (Elwert/Winship 2013)
 - Truncation and censoring
 - Missing data (non-response depending on outcome or collider)
 - Selection bias in the Heckman sense
 - Panel attrition
 - Social contagion in networks
 - \rightarrow not only an exceptional case, but a widespread problem



Sample selection on the dependent variable

- Actually an unproblematic model
- But if only a part of the value range of Y can enter the sample then a back-door path opens up
- Example: Truncation of income (no "high earners" in the sample)

Survey Non-Response

 Survey non-response can produce an apparent correlation if both T and Y influence the response E.g., education and income





Source: Brüderl Slides Causal Analysis

Illustration: Berkson's paradox

- RQ: Does stronger networking of researchers increase publication output?
- Additional assumption: Both factors increase the chance of obtaining a professorship.
- Hypothetical causal structure:



Simulation: a) Networking & publications each exponentially distributed.

b) Networking & publications uncorrelated

c) Networking, publications & random factors influence p(professorship)(31.7%)

Illustration: Berkson's paradox

		Model 2			
DV: number of publications	Whole population	Professor	No professor	Whole population	
Network size	0,0004 (-0,31)	-0,025*** (-8,91)	-0,090*** (-11,52)	-0,031*** (-12,48)	
Academic status (1 = Professor)				4,858*** (-15,32)	
Constant	9,029*** (-85,45)	13,070*** (-35,74)	9,619*** (-71,81)	8,911*** (-85,08)	
N	10.000	3.168	6.832	10.000	
R ²	0,00001	0,025	0,019	0,023	
Adj. R ²	-0,00009	0,024	0,019	0,023	

Mediator: well-known, but often mishandled

Mediators

- Pearl: indirect effect via front-door pathway
- Example with direct and indirect effect



- Desirable because
 - deeper understanding of generative mechanisms (especially important for impact evaluation and transfer of measures)
 - Sometimes: only possibility to identify causal effects

Mediator: well-known, but often mishandled

Unfortunately, a too-common misunderstanding:



If there is an effect of T on Y, which is disappears after controlling for M, this does <u>not</u> mean that T has no effect on Y.

It means, T has <u>no direct</u> effect on Y and that all/most of the total effect flows through M (<u>indirect</u> effect).

Example: Physical appearance & job interview invites

Job vacancies

Editor for a Magazine in the Area of [Automotive / Home Ideas & Decoration]

Our company is a renowned specialized publisher based in Nuremberg. In our house, a monthly magazine is released with a focus on [automotive / home ideas & decoration].

<u>Tasks:</u>

- Writing own articles and reports as well as proofreading contributions
- Idea generation and conception of relevant new topics
- Coordination within the editorial team

Required Qualifications:

- Several years of experience in the conceptual and practical production of magazines
- Extensive specialist knowledge
- High degree of autonomy
- Reliability
- Leadership and social skills

Deepfaked application videos



Probability (invite to interview)



Kühn & Wolbring, 2024

Example: Physical appearance & job interview invites

	(1)	(2)	(3)
	Treatment	incl. Controls	incl. Competence
Ref: Less attractive applicant			
More attractive applicant	5.717** [1.41,10.02]	5.797** [1.42,10.17]	0.345 [-2.98,3.67]
Ref: Male applicant			
emale applicant	-5.197* [-9.þ2,-0.87]	-5.400* [-9.77,-1.03]	-6.755*** [-10.08,-3.43]
Ref: Home Ideas & Deco			
Automobile	1.662 [-2.62,5.94]	1.849 [-2.45,6.15]	1.142 [-2.02,4.30]
Aore attractive applicant Female applicant			
ndex of Competence			14.774*** [12.97,16.58]
Controls: Respondent gender, age, hiring xperience		included	included
Constant	70.056***	70.166***	-6.198
	[65.61,74.51]	[57.88,82.45]	[-19.99,7.59]
Observations	493	493	493
R ²	0.027	0.036	0.454
Adjusted R ²	0.021	0.016	0.442

Kühn & Wolbring, 2024

Open and blocked paths

Structural positions of covariates

- Mediator → Risk of over-control (if interested in total effect)
- Confounder \rightarrow Risk of under-control
- Collider \rightarrow Risk of over-control

ightarrow Affects how to deal with covariates



Different identification strategies

Identification by design: exogenous variation in the treatment

Identification by design with the prototype "experiments" with three features:

- (1) At least one treatment and one control group
- (2) Active intervention researcher has control over treatment assignment
- (3) Random assignment of treatment
- \rightarrow Treatment assignment by mechanism D is exogenous: $(Y^0, Y^1) \perp D$



→Other identification strategies such as instrumental variables, natural experiments, and regressiondiscontinuity designs try to mimick the experimental approach

Identification by back door conditioning

Back door conditioning is most common with observational data. The idea is to close all the open back door paths.

If all open back door paths closed, the CIA holds.



Identification via front door paths

Mediators

- Basic idea: 3-stage procedure
 - 1) Estimation of the effect T \rightarrow M
 - 2) Estimation of the effect M \rightarrow Y
 - 3) Combining estimates 1) and 2)

Important assumption: Isolability of mechanisms

- \rightarrow often unrealistic in practice (also in experiments)
- → Current debate on appropriate methods and designs, mainly influenced by Pearl's perspective (e.g. in Psych. Methods; blog update by David A. Kenny in October 2013)



Identification via front door paths

Mediators: A more complex example

• Motherhood and Wages



Quelle: Knight/Winship 2013

Part C DAGs in action

Application

Weight & Wages

Economics and Human Biology 9 (2011) 356-363



Fat, muscles, and wages

Christiane Bozoyan^{*}, Tobias Wolbring¹ LMU Munich, Institute of Sociology, Konradstraße 6, 80801 Munich, Germany

European Sociological Review, 2018, 1–14 doi: 10.1093/esr/jcy009 Original article

OXFORD

The Weight Wage Penalty: A Mechanism Approach to Discrimination Christiane Bozoyan¹ and Tobias Wolbring^{2,*}

Schmollers Jahrbuch 135 (2015), 83–96 Duncker & Humblot, Berlin

The Usefulness of Directed Acyclic Graphs: What Can DAGs Contribute to a Residual Approach to Weight-Related Income Discrimination?*

By Christiane Bozoyan and Tobias Wolbring

Weight and wages

Theoretical estimand

Body weight • Income



Causal Identification of empirical estimand

You consider to include the following variables in the model for causal identification:

- Gender (male/female/other)
- Age (in years)
- Customer contact of job (yes/no)
- High school education (yes/no)
- Marital status (married/ not married)

However, before you estimate the model, you want to draw a DAG for these variables to make sure you get the model right.

Weight and wages

Causal Identification of empirical estimand



You consider to include the following variables in the model for causal identification:

- Gender (male/female/other)
- Age (in years)
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- Marital status (married/ not married)

However, before you estimate the model, you want to draw a DAG for these variables to make sure you get the model right.

DAGitty — draw and analyze causal diagrams

Software to facilitate covariate selection

- <u>www.dagitty.net</u> (Knüppel/Stang 2010; Textor et al. 2011)
- all minimal subsets of covariates whose control is sufficient to identify the causal effect (minimal sufficient adjustment sets).

DAGitty — draw and analyze causal diagrams



DAGitty — draw and analyze causal diagrams

dag { bb="0,0,1,1" "Body weight" [exposure,pos="0.198,0.378"] "Customer contact" [pos="0.413,0.190"] "Marital status" [pos="0.420,0.074"] Age [pos="0.420,0.579"] Education [pos="0.420,0.688"] Income [outcome,pos="0.579,0.381"] "Body weight" -> "Customer contact" "Body weight" -> "Marital status" "Body weight" -> Income "Customer contact" -> Income "Marital status" -> Income Age -> "Body weight" Age -> Income Education -> "Body weight" Education -> Income

Weight and wages

Theoretical estimand



Empirical estimand

You consider to include the following variables in the model for causal identification:

• Gender (male/female/other)

• ...

 \rightarrow Think about the causal structure, draw a causal graph and analyze it (e.g. with DAGitty).

Estimation

- Do you compare means? Or do you run a regression?
- How do you operationalize the variables? (e.g., dummy for obesity, hourly wage)
- Do you log Y? Do you use polynomes for age?

Time for an exercise

Exercise

Please analyze the following graph with your seat neighbour(s).

A1) What do you need to control for estimating the total causal effect of T on Y?
A2) What do you need to control for estimating the direct causal effect of T on Y?
A3) There is a way to determine the indirect effect via M1. Any idea how you could do it?



Note: The example could be the effect of having kids on wages. The two mediators could be biases by employers and effort by employees.

Exercise

B1) Please analyze the following graph by visual inspection. Which variables would you control to estimate the effect of T on Y?



B2) Now draw the same graph in DAGitty and interpret the output of DAGitty with respect to potential control variables.

Graph for exercise B

dag { bb="0,0,1,1" T [exposure,pos="0.212,0.477"] X1 [pos="0.205,0.111"] X2 [pos="0.496,0.099"] X3 [pos="0.208,0.301"] X4 [pos="0.374,0.298"] X5 [pos="0.506,0.302"] X6 [pos="0.368,0.482"] Y [outcome,pos="0.518,0.480"] T -> X6 X1 -> X3 X1 -> X4 X2 -> X4 X2 -> X5 X3 -> T X4 -> T X4 -> Y X5 -> Y X6 -> Y

}

Exercise

We want to identify the causal effect of D on Y

C1) Which paths are causal? Which paths are non-causal (backdoor paths)?

C2) Which backdoor paths are open? Which are closed?



Graph for exercise C

dag { bb="0,0,1,1" D [exposure,pos="0.218,0.493"] V [pos="0.496,0.266"] W [pos="0.358,0.671"] Y [outcome,pos="0.587,0.488"] Z [pos="0.291,0.267"] D -> V D -> W D -> Y W -> Y Y -> V Z -> D Z -> V Z -> Y

}

Summary

- Graph methodology as a link between theory and statistical analysis
- Clear explication of the assumptions and the limits of identification
- Both risk of under-control and over-control
 - \rightarrow no "control everything" strategy, but need to think about causal structure



Recommended reading

- Cinelli, C., Forney, A., & Pearl, J. (2024). A Crash Course in Good and Bad Controls. Sociological Methods & Research, 53(3), 1071-1104.
- Elwert, Felix (2013): Graphical Causal Models. In: Morgan, Stephen L. (Hg.): Handbook of Causal Analysis for Social Research. Dordrecht: Springer, S. 245-273.
- Elwert, Felix/Winship, Christopher (2014): Endogenous Selection Bias: The Problem of Conditioning on a Collider Variable. Annual Review of Sociology 2014 40:1, 31-53.
- Morgan, Stephen L./Winship, Christopher (2015): Counterfactuals and Causal Inference. Methods and Principles for Social Research. 2. edition. Cambridge, MA: Cambridge University Press.
- Schuessler, J., & Selb, P. (2023). Graphical Causal Models for Survey Inference. Sociological Methods & Research, 1-32. <u>https://doi.org/10.1177/00491241231176851</u>

Recommended reading: more comprehensive treatments

Hernán MA, Robins JM (2020). Causal Inference: What If. Boca Raton: Chapman & Hall/CRC."

- Pearl, Judea (2009): Causality: Models, Reasoning, and Inference. Cambridge: Cambridge University Press (2. ed.).
- Pearl, Judea, Glymour, Madelyn and Nicholas P. Jewell (2016) Causal Inference in Statistics: A Primer, Wiley.
- Pearl, Judea and Dana Mackenzie (2018): The Book of Why: The New Science of Cause and Effect, New York: Basic Books.
- VanderWeele. T.J. (2015). Explanation in Causal Inference: Methods for Mediation and Interaction. Oxford University Press.

Recommended reading: DAGitty

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Thank you for your attention!

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